Semantic Photometric Bundle Adjustment on Natural Sequences

Rui Zhu, Chaoyang Wang, Chen-Hsuan Lin, Ziyan Wang, Simon Lucey
The Robotics Institute, Carnegie Mellon University
{rz1, chaoyanw, chenhsul, ziyanwl}@andrew.cmu.edu, slucey@cs.cmu.edu

Abstract

The problem of obtaining dense reconstruction of an object in a natural sequence of images has been long studied in computer vision. Classically this problem has been solved through the application of bundle adjustment (BA). More recently, excellent results have been attained through the application of photometric bundle adjustment (PBA) methods – which directly minimize the photometric error across frames. A fundamental drawback to BA & PBA, however, is: (i) their reliance on having to view all points on the object, and (ii) for the object surface to be well textured. To circumvent these limitations we propose semantic PBA which incorporates a 3D object prior, obtained through deep learning, within the photometric bundle adjustment problem. We demonstrate state of the art performance in comparison to leading methods for object reconstruction across numerous natural sequences.

1. Introduction

In this paper we are primarily concerned with the goal of obtaining dense 3D object reconstructions from short natural image sequences. One obvious strategy is to employ classical bundle adjustment (BA) [18] across the sequence where we can simultaneously recover camera pose and 3D points. Although reliable, this strategy is problematic as it: (i) can only recover 3D points if they are observed in the image sequence, and (ii) the density of the reconstruction is dependent on how textured the surface of the object is across the image sequence. Recently, photometric extensions to bundle adjustment have been proposed [1, 4] that directly minimize the photometric consistency between frames with respect to pose and 3D points. Borrowing upon the terminology of [1] we shall refer to these methods collectively herein as photometric bundle adjustment (PBA). PBA has recently proved advantageous over classical BA for problems where dense reconstructions are required due to their ability directly minimize for photometric consistency. Even with these recent innovations PBA is still, however, fundamentally limited in performance by (i) and (ii).

There have been numerous efforts within the computer vision community to bring semantic prior into the task of object/scene 3D reconstruction. Convolutional Neural Networks (CNN) are proving remarkably useful for this task when one is provided with scene [17, 24] or object category [25, 7] specific labels & priors. A powerful characteristic of these semantic CNN methods is their ability to circumvent the fundamental limitations of (i) and (ii). For example, [25, 7, 21, 6] offer strategies for inferring a dense 3D reconstruction of an object from a single image even when a substantial portion of the projected 3D points are self-occluded. More recently, semantic CNN strategies have been proposed that attempt to incorporate multiple frames [3, 9]. Most of these previous efforts have been
trying to attack the problem of 3D reconstruction as a supervised learning problem – where geometry is largely treated as a label to be predicted.

Although attractive in its simplicity this strategy has some inherent drawbacks. First, these geometric labels can be problematic to obtain – hand labeling can be error prone, and rendering can lack the necessary realism. Second, the predicted labels from these network models do not adhere to geometric constraints – such as photometric consistency – making the results unreliable. Recently, the application of geometric constraints within the offline CNN learning process has been entertained including reprojected silhouette matching [22, 25], depth matching [14], and even photometric consistency [19, 13, 12]. A fundamental problem with these emerging methods, however, is that the geometric constraints are not enforced at test time – dramatically reducing their effectiveness.

Given these concerns, we argue that instead of incorporating geometric constraints into semantic CNN strategies offline, one should instead incorporate object semantics within the PBA pipeline. As we demonstrate in Fig. 1 and our results section this strategy gives the best of both worlds – semantic knowledge of the object with photometric consistency. In this paper, we propose an enhanced semantic PBA method which works on natural sequences as the classic PBA does, and give extensive evaluations on both synthetic and natural sequence domains. We summarize our contributions as follows:

- We provide the first approach of its kind (to our knowledge) for semantic object-centric PBA on natural sequences – which gives the global 6DoF camera poses of each frame and the dense 3D shape, with PBA-like accuracy but denser depth maps.
- We systematically evaluate the local optimality of our proposed optimization pipeline, as well as our enhanced objective which takes use of classic PBA results as off-the-shelf initialization or regularizer in our method.
- We collect a new dataset for the task of object-centric shape reconstruction, consisting of rendered sequences of full ground truth in cameras, depth maps, and the shape in canonical pose, as well as natural sequences annotated with ShapeNet [2] models, making the dataset feasible for evaluating both PBA methods with camera estimations [11, 8], and methods which only recover aligned shapes or depth maps [20, 13, 9] by end-to-end learning on ShapeNet.

1.1. Related Work

Photometric Bundle Adjustment: Photometric bundle adjustment (PBA) which is an optimization based method sitting entirely upon the visual cue of photometric consistency across all input frames [5, 15, 11]. In PBA the shape is recovered by jointly optimizing for depth maps corresponding to the visible pixels in template frames [5, 15, 11], as well as camera motion. As a result the formulation of classic PBA is solely to recover the geometry of the scene, completely agnostic to semantics of the scene/object. Some works in PBA aims for small motion videos in particular [11, 10].

Shape Reconstructing with Deep Learning: As previously mentioned, early deep learning methods [7, 21, 6, 3, 9] solve the task of object-centric (object shape only) reconstruction with supervision from shape labels. Recently, an emerging school of thought seeks to bring in geometry back to the task, including reprojected silhouette matching [22, 25], depth matching [14], and even photometric consistency [19, 13, 12]. One issue of most of these methods is they assume known cameras, in global frame. This is in fact a too strong assumption to hold for natural sequences where global camera poses are not readily available. While some others do not account for camera motion at all [20, 3], which creates a gap from classic PBA where camera motions are instead the direct output.

Semantic PBA: Recent work of Zhu et al. [26] also proposed to apply shape priors within PBA for 3D object reconstruction. In spite of the similarity in the formulation of the problem, Zhu et al.’s approach was problematic in a number of ways. First, the performance of Zhu et al. relies heavily on the initialization point given by CNN pose/style predictors trained predominantly on rendered images, which is suspicious for its reliability on natural sequences. Instead, we utilize a more reliable source – relative camera pose from PBA for initialization. Second, due to the limitations of the method, such as weak perspective camera model assumption and unreliable initialization source, Zhu et al.’s evaluation was restricted to rendered sequence. Thus they did not conduct quantitative comparisons between actual PBA methods [11, 8] w.r.t. camera pose error or depth error on real world sequences; while we give an extensive evaluation of our method on real sequences. Third, Zhu et al. did not give a proper analysis of the characteristics of their objective function, which results in using inadequate optimization techniques for their approach; In this paper, through inspecting the property of different cost functions, we propose a more robust and efficient optimization pipeline.

Notation: Vectors are represented with lower-case bold font (e.g. a). Matrices are in upper-case bold (e.g. M) while scalars are lower-cased (e.g. a). Italicized upper-cased characters represent sets (e.g. S). To denote the $i^{th}$ sample in a set (e.g. images, shapes), we use subscript (e.g. $M_i$). Calligraphic symbols (e.g. $\pi$) denote functions. Images are defined as sampling function over the pixel coordinates, i.e. $I(u) : \mathbb{R}^2 \rightarrow \mathbb{R}^3$. 
2. Approach

2.1. Preliminary

Camera model We assume a perspective camera with known intrinsics $K$. The camera extrinsics are parameterized as concatenation of exponential coordinates (also known as twist) of rotation and translation vector: $p = [\omega; t] \in \mathbb{R}^6$. The camera projection function is written as

$$\pi(x; p) = K(R(\omega)x + t). \quad (1)$$

Given a short window of $L$ frames as in PBA [11, 1], we define the first frame as the target frame (frame 0), and the subsequent $L - 1$ frames as source frames. The relative camera pose between the target frame and source frame is denoted as $\Delta p_l = [\Delta \omega_l; \Delta t_l]$. The global pose is thus computed as a composition of relative pose of the source frame and the global pose of the target frame:

$$p_l = [\Delta \omega_l \circ \omega_0; \Delta t_l + t_0]. \quad (2)$$

We define the pose composition rule as:

$$R(\Delta \omega \circ \omega) = R(\Delta \omega)R(\omega), \quad \Delta t \circ t = \Delta t + t. \quad (3)$$

The reprojection of one point $x$ onto frame $l$ with the corresponding global pose is framed as sampling the image with reprojected pixel location $I_l(\pi(x_l; p_l))$.

Reprojection with pseudo-raytracing Reprojection from a point set $X$ given camera pose $p$ can be viewed as first reasoning the visible part of the point set with a masking function $X_p := \mathcal{M}(X; p)$ where $X_p = \{x_j\}_{j=1}^{M_p}$. The mask function is implemented as pseudo-raytracing [14] by projecting the points to a enlarged inverse depth plane by a factor $U$, and then perform max pooling in a neighbourhood of $U \times U$ to figure out the visible point with biggest inverse depth. By doing so the mask function gives both the indices of the $M_p$ visible points, and an inverse depth map.

2.2. Overview

Our method takes in a RGB sequence taken by a calibrated camera moving around an object. The category (e.g. cars, airplanes, chairs) of the object is assumed to be known, and we have a rich repository of aligned CAD models (e.g. ShapeNet [2]) for this category. We define the world coordinate system as one attached to the objects as chosen by the CAD dataset, and the calibrated perspective camera model is parameterized by full 6DoF rotation and translation (see Fig.2). The goal of our method is to recover the full 3D shape of the object in the world frame, as well as the 6DoF parameters of the camera pose of each frame.

We adopt the category-specific shape prior from Zhu et.al [26] to learn a shape space from the repository of ShapeNet [2] CAD models. We use dense point cloud as the shape parameterization in our work, considering learning shape space of point clouds has been made possible by several works [6, 16, 26]. The shape prior is a learned category-specific point cloud generator, written as a function of a style vector $s \in \mathbb{R}^S$ which represents the sub-category object style. The output of the shape prior is the set of gener-
ated points defined as $X := \{x_i\}_{i=1}^N = \mathcal{G}(s)$. For the $6\text{DoF}$ poses of the total $L$ frames, we break the pose parameters into two sets: the global camera pose of the target frame $p_0 \in \mathbb{R}^6$, and the relative camera pose between each source frame and the corresponding target frame $\{\Delta p_i \mid i=1, \ldots, L\}$.

The overall pipeline of our method is illustrated in Fig. 2. We formulate the inference of the style vector and camera pose parameters as optimization steps with geometric objectives. The parameters are initialized with an off-the-shelf initialization pipeline (see 2.4), and the optimization steps are taken to minimize this objective over the parameter space. In this paper, we propose to take advantage of the cheap and rough outputs from other methods to regularize our optimization procedure. For each frame, we get cheap segmentation masks (silhouettes) from recent state-of-the-art instance segmentation method FCIS [23]. Considering traditional PBA methods gives as results semi-dense inverse depth and camera motion, we also borrow the readily available although error-prone outputs from PBA pipelines (e.g. openMVS [8]) to add another inverse depth loss with the estimated depth. We also take advantage of their camera motion estimation to initialize the relative camera pose of each source frame w.r.t. its target frame.

### 2.3. Optimization Objective

**Photometric Consistency** The basic objective is formulated as the photometric consistency between the corresponding pixel pairs from the target frame and each source frame. Classic PBA methods usually track a set of sparse points through all the frames in a window, while with our formulation we are able to get dense correspondence automatically derived from reprojection. Considering that visible points may differ in each frame due to camera motion and occlusion, in this work we formulate the bi-directional photometric consistency as:

$$\mathcal{L}_{\text{ph}}(p_0, \{\Delta p_i\}_{i=1}^{L-1}, s) = \frac{1}{L} \sum_{l=0}^{L-1} \left( \sum_{u_k \in U_{l+1}} \min_{u_j \in U_l} ||u_k - u_j||^2_2 \right) + \sum_{u_j \in U_l} \min_{u_k \in U_{l+1}} ||u_j - u_k||^2_2.$$  

Finally, apart from cheap camera motion, we are able to get semi-dense depth map for each frame from the off-the-shelf PBA pipeline. In this case we further formulate the extra objective term of inverse depth error as:

$$\mathcal{L}_{\text{invd}}(p_0, \{\Delta p_i\}_{i=1}^{L-1}, s) = \frac{1}{L} \sum_{l=0}^{L-1} \mathcal{L}_{\text{invd}}(d'_l - \alpha d_l)$$

where $d_l$ is given by our reprojection module. Note that $\alpha$ here should be updated on the fly. Considering we will be getting confident camera poses for all frames in a few optimization steps, $\alpha$ can be robustly solved by finding a scale that best aligns the estimated camera poses with the ones from the offline estimator. Specifically, we can solve for an $\alpha_l$ for each source frame $l$:

$$\begin{align*}
\begin{cases}
\mathcal{R}_0(\omega_0)x + t_0 = \alpha_l \left( \mathcal{R}'_0 x + t'_0 \right) \\
\mathcal{R}_l(\omega_l)x + t_l = \alpha_l \left( \mathcal{R}'_l x + t'_l \right)
\end{cases}
\end{align*}$$

The solution for $\alpha$ is average over all $\{\alpha_l\}_{l=1}^{L-1}$:

$$\alpha = \frac{1}{L-1} \sum_{l=1}^{L-1} \arg \min_{\alpha} ||\mathcal{R}_l(\omega_l)x + t_l - \mathcal{R}'_l \mathcal{R}_0^T(\omega_0)x + t_0 - \alpha(t'_l - \mathcal{R}'_l \mathcal{R}_0^T t'_0)||^2_2.$$  

The combined objective is given by:

$$\mathcal{L} = \mathcal{L}_{\text{ph}} + \lambda_1 \mathcal{L}_{\text{cad}} + \lambda_2 \mathcal{L}_{\text{invd}},$$

where ablative study about the weight factors $\lambda_1$ and $\lambda_2$ is included in the Appendix.

### 2.4. Initialization

**Style and Pose Initialization** We improve upon existing learning-based pipeline to provide initialization for style and template frame camera pose. For style, unlike [25, 26] where a single-image based regressor is adopted, we use a recurrent network architecture to leverage the sequential information in an effort to alleviate ambiguity in style from a single viewpoint. Details about the architecture of our regressor and the training process as well as dataset are included in the Appendix. To generate more accurate style
Figure 3: Local cost surface of \( p_0 \) and \( \Delta p_l \). The yellow dot marks the optimum while the yellow line shows the search space for \( p_0 \) if \( \Delta p_l \) is initialized with offline camera motion.

vectors, we exploit cheap silhouette from Li et al. [23] to mask off the background.

To find a coarse pose initialization, we first utilize BlenderTM to render templates under varying camera poses. After that we retrieve a coarse pose by finding one template which has the maximum IoU with the target silhouette.

**Camera Motion Initialization** One observation of ours is, the photometric consistency error is problematic in our optimization of the objective. On the one hand \( L_{ph} \) is locally bi-linear with Gauss-Newton solvers, where in traditional PBA the template term is fixed so that the residual is linear and the problem is locally convex. The problem is worsened in the way the variables are initialized as in Zhu et al. [26], where \( \{ \Delta p_l \}_{l=1}^{L-1} \) are initialized to all zeros when we have a poorly-initialized \( p_0 \). To illustrate this we show in Fig. 3 by plotting the cost surface over local perturbation of \( p_0 \) and \( \Delta p_l \). We show that the cost surface is highly non-convex between the initialization and the optimum if both variables are initialized far from the ground truth (red arrows). However we show with the camera motion parameters initialized correctly, the search space of \( p_0 \) is constrained to the yellow line with better curvature for better convergence (green arrows).

Inspired by this observation, at the beginning of our pipeline we run an off-the-shelf PBA pipeline (e.g. [8]) to acquire camera poses \( \{ p_l \}_{l=0}^{L-1} \) for every frame, as well as a semi-dense point cloud \( X' \). By formulation we have the following relation between our camera model (left) and the off-the-shelf estimator (right):

\[
R_l(\omega_l)x + t_l = \alpha \left( R'_l(\omega'_l)x' + t'_l \right).
\] (10)

Unfortunately no correspondence between \( x \) and \( x' \) is available to give an accurate estimation of the scale factor \( \alpha \). Instead we seek to bring the estimation of \( \alpha \) in the loop by aligning the estimated inverse map \( d'_0 \) to our reprojected inverse depth \( d_0 \):

\[
\arg\min_{\alpha} ||d'_0 - \alpha d_0||^2_2.
\] (11)

The camera motion is then initialized by solving:

\[
\begin{align*}
\Delta R_l(\Delta \omega_l) &= R'_l R_0^T \\
\Delta t_l &= R'_l R_0^T t_0 + \alpha \left( t'_1 - R'_l R_0^T t'_0 \right).
\end{align*}
\] (12)

We use Equ. 13 for initializing the camera motion parameters before the optimization steps.

### 2.5. Optimization Pipeline

Given reasonable initialization from the above steps, we solve our objective with gradient-descent based methods. Particularly we found off-the-shelf L-BFGS solver gives efficient solution to our problem. We summarize our optimization pipeline in Algorithm 1.

**Algorithm 1** Optimization of the objective

1. **procedure** \( \mathcal{L}(p_0, \{ \Delta p_l \}_{l=1}^{L-1}, s) \)
2. \( p_0, s \leftarrow \text{Initialize}(I_0) \)
3. \( \alpha, \{ \Delta p_l \}_{l=1}^{L-1}, \{ d'_l \}_{l=0}^{L-1} \leftarrow \text{openMVS} [8], \) Equ. 13
4. while \( \mathcal{L} > \delta_L \) or step < maximum iterations do
5. \( p_0 \leftarrow \text{L-BFGS update on } p_0 \)
6. \( \{ \Delta p_l \}_{l=1}^{L-1} \leftarrow \text{L-BFGS update on } \{ \Delta p_l \}_{l=1}^{L-1} \)
7. \( s \leftarrow \text{L-BFGS update on } s \)
8. \( \alpha \leftarrow \text{Update on } \alpha \text{ by Equ. 8} \)
9. **return** \( \{ p_0, \{ \Delta p_l \}_{l=1}^{L-1}, s \} \)

### 3. Evaluation

#### 3.1. Data Preparation

**Rendered Data** To enable evaluation of our methods against Zhu et al. [26] which is only feasible on rendered domain, we follow Zhu et al. by rendering small baseline sequences from ShapeNet [2] cars. Please refer to Appendix for the statistics which is inherently identical to Zhu et al. apart from our perspective camera versus weak-perspective by Zhu et al.
Natural Data In view of the absence of object-centric and category-specific natural video dataset, we collect our own test set with a mixture of sequences from toy model cars and real cars. We carefully choose the models with ground truth CAD available in ShapeNet [2]. Each video is shot with iPhone 6s (30fps) with around 30 ° of rotational motion and moderate translation, and the images are scaled down to 512 × 512. There are 15 videos collected from 4 toy car models and 12 videos from 6 real cars for evaluation. For each sequence, we annotate the template frame and last frame with ground truth CAD models and 6DoF pose. Samples of our test data can be found in Fig. 4.

We also visualize some qualitative results of our initialization on natural sequences in Fig. 4. Although the style retrieved from regressor is not very precise in color or details, our style regressor is able to yield style prediction that are close in 3D shape.

3.2. Evaluation on Rendered Sequences

In this section, we give both qualitative and quantitative results of our methods against 1) classic PBA methods of open-source openMVS [8], and Ham et al. [11] which is a PBA pipeline specifically optimized for small motion videos, 2) learning based methods [6, 3] which gives shapes in canonical poses.

In our experiments, we set the weights in the optimization objective as \( \lambda_1 = 0.1 \) with \( \delta_1 = 100 \) (we use unnormalized RGB values in range [0, 255]), and \( \lambda_1 = 1000 \) with \( \delta_2 = 10 \). Ablative study on different settings of the hyper-parameters is included in the Appendix.

Since we are evaluating on synthetic sequences from Blender™, we have access to full ground truth for both the camera pose of every frame (in world coordinate system), as well as the ground truth dense depth map and dense shape. However given our formulation is to output full 3D shape in an object-centric manner, while openMVS and Ham et al. give semi-dense point cloud of the entire scene by best effort, we are not able to align three outputs to the ground truth shape. Instead we choose to follow Ham et al. [11] to measure the depth error of the recovered points by re-projecting the shape onto the image plane with the estimated cameras. To compare with openMVS [8] and Ham et al. [11] which give only relative camera motion of every source frames w.r.t. to the first frame, we offer ground truth camera pose of the first frame to these two methods and find a rigid-body transformation to align their camera pose of the first frame to the ground truth. The scale ambiguity is solved by Equ. 8. By doing this, the shape and camera poses of all methods are ideally aligned to the world coordinate system, and we are able to measure the camera error by calculating the camera position error as the distance of the estimated camera center to its ground truth, and the camera orientation error as the acute angle between the estimated camera orientation and its ground truth.

We report the average error of depth maps and camera poses in Table 1 and the statistics in Fig. 6. The results show that our method achieves comparable camera error as openMVS [8], but slightly worse than Ham et al. [11] which is specifically optimized for small motion videos for better camera tracking. For the depth map error we achieve SLAM-like performance by outperforming both openMVS [8] and Ham et al. [11] in addition to much denser results thanks to the shape prior which produces full 3D shapes.

Moreover, again thanks to the shape prior, we show in Fig. 7 that we only need a few observations of the object to give confident results, even at two frames, while classic methods [8, 11] start at considerable amount of motion to perform camera tracking.

Finally we experiment on all the rendered sequences by perturbing upon their ground truth \( p_0 \) and calculate the average \( p_0 \) at convergence. We show in Fig. 8 that our method achieves better convergence in face of large initialization error in pose.

3.3. Evaluation on Natural Sequences

We evaluate our methods against others on the object-centric dataset we collected. The dataset includes sequences of a mixture of toy cars and real cars. The sequences are annotated with aligned CAD models retrieved from the ShapeNet dataset [2]. Considering it is not possible to get the 6DoF camera poses for all frames through human annotation, we evaluate on the depth error of the annotated first frame of each sequence, as well as the density of the re-projected points against the ground truth. The quantitative
Figure 5: Results of our methods on natural sequences, and comparison with openMVS [8], Ham et al. [11], and deep learning based methods [3, 6]. For openMVS [8] and Ham et al. [11] we align the cameras to the world coordinate frame (note that our method automatically produces camera poses in world frame), and we draw the aligned shape, estimated camera trajectory (blue) with orientation (red), annotated camera (black) of two frames (marked with black dot). We also project the shape with the estimated camera, and color the reprojected points with their inverse depths (brighter is closer). In the last row we show for each sample results from 3D-R2N2 [3] (left) and Fan et al. [6] (right).

results are reported in Table 1. We also show qualitative results on 4 natural sequences (2 model cars plus 2 real cars) in Fig. 5. Each sequence consists of \( L = 91 \) frames with roughly 30 degree of camera rotation and moderate translation. We show that we achieve comparable camera poses and denser inverse depths against openMVS [8] and Ham et al. [11]. Additionally ours recovers semantic information including full 3D shape detached from the map, and again global cameras. For sequence 3 and 4 Ham et al. [11] gives degraded solution when it fails at camera tracking or deification due to little motion in frame 3 or significant lighting change in sequence 4. We attempt to give part of its results
<table>
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<th>Cam. Location Error</th>
<th>Cam. Orientation Error</th>
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<td>Ham et al.</td>
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<td><strong>0.9342</strong></td>
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<td><strong>1.2343°</strong></td>
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</tbody>
</table>

Table 1: **Quantitative comparison on both rendered and natural sequences.**

Figure 6: **Depth error on the rendered test set.** On the left axis shows the histogram of depth error distribution, and on the right axis gives the percentage of pixels under the threshold.

Figure 7: **Depth error on the rendered test set.** On the left axis shows the histogram of depth error distribution, and on the right axis gives the percentage of pixels under the threshold.

We also notice that learning based methods [6, 3] which are mostly trained on rendered images suffer from the domain gap in our test natural sequences.

4. Conclusion

In this paper we propose the method of semantic photometric bundle adjustment for object-centric shape reconstruction from natural sequence, which exerts geometric constraints over the camera pose as well as the full 3D shape generated by a learned semantic shape prior. We extensively evaluate our approach on both rendered and natural settings against both classic PBA methods and deep learning based methods, and prove that it is capable to produce dense full 3D shape in world coordinates, as well as depth maps of PBA-like quality.

References


Supplementary Material
Semantic Photometric Bundle Adjustment on Natural Sequences

Rui Zhu, Chaoyang Wang, Chen-Hsuan Lin, Ziyan Wang, Simon Lucey
The Robotics Institute, Carnegie Mellon University
{rz1, chaoyanw, chenhsul, ziyanw1}@andrew.cmu.edu, slucey@cs.cmu.edu

1. Appendix I. Data Preparation

1.1. Point Clouds for Learning the Shape Prior

We utilize the large-scale shape dataset ShapeNet [2] for learning our point-cloud-based shape prior. For the “car” category, we sample each CAD mesh in the training set (5,996 models in total) with uniform sampling tool from the Point Cloud Library [12]. Each model is pre-aligned and normalized to fit within a cubic space of 1 unit along each axis, centering at the origin point of the world coordinate system.

1.2. Rendered Sequences for Learning the Style Regressor

For training our style regressor, we construct a rendered object-centric short sequence dataset following the settings of Zhu et al. [14]. To mimic the camera pose distribution of the natural sequences which we collect for testing, which normally feature considerable rotational motion, almost centered object and small elevation, we sample the initial elevation and yaw within $[-3^\circ, 8^\circ]$ and $[-5^\circ, 5^\circ]$ respectively while azimuth lying in $[0^\circ, 360^\circ]$, and we span the motion in azimuth approximately over $30^\circ$. In addition, a noise term from uniform distribution $U[-1^\circ, 1^\circ]$ is applied to azimuth, elevation and yaw for modeling camera shake. For training, we use the total 5,996 instances in the “car” category from ShapeNet. The remaining 1,500 instances in car category form the validation set. For each model, we render 100 short sequences with different initial camera poses. In total the training set consists of 599,600 sequences with 8,994,000 frames and the testing set has 1,500 sequences and 22,500 frames.

1.3. Rendered Sequences for Evaluation

Rendered sequences provide full ground truth on both the shape, depth maps, and the camera poses, which makes them ideal test set to compare both our methods and classic PBA methods upon. We largely follow the data preparation procedure above to prepare the rendered sequences for evaluation. We rendered one sequence with 90 frames at resolution 512×512 for the first 20 model in the test set with sampled camera motion and lighting condition. We do not evaluate on all 1,500 models because all methods are optimization-based during inference, which usually takes up to 10 minutes for one sequence. This makes it impossible to give comprehensive statistical analysis on all the 1,500 models in the ShapeNet test set. To evaluate classic PBA methods [4, 6] which implement feature-based camera tracking, we utilize the full-length high-resolution sequences as their inputs. For our methods as well as Zhu et al. [14], considering we do not rely on feature-based camera tracking, we down sample each sequence to 15 frames as the inputs.

2. Appendix II. Evaluation Details

2.1. Rendered Sequences

We evaluate all methods on the rendered test set which we introduced earlier to give a quantitative comparison on both depth maps and camera poses in Table 1 in the main body of the paper.

Performance against Varying Views In Fig. 7 in the main body of the paper, we vary the number of input views from 1 to 90 for all of the methods, and average the depth error and depth density over all sequences to demonstrate how the performance change over the number of views available.

Robustness Against Initialization Error In Fig. 8 in the main body of the paper, we compare our methods against Zhu et al. [14] on one of the initialization variables – the initial pose of the template frame $p_0$. The result is again averaged over all test sequences.

Sample results on our natural sequence test set can be found in Fig. 1.

2.2. Natural Sequences

More results on our natural sequence test set can be found in Fig. 2. We also include two videos (named demo_comparison_{6, 15}fps.mp4) in the Supplementary Material showing panoramic view of the shapes and camera as well as reprojection onto each frame, between our
Figure 1: **Sample results of rendered sequences.** For each sample sequence, we show the first and last frame of the sequence (first row), the recovered shape and camera poses in two views (middle row) and the reprojected points onto the first and last frame, colored with the inverse depths (brighter is closer). For the recovered shape, we color the visible points with pixel values from the frames, and the invisible points with grey.

We follow the same coloring scheme as Fig. 1 and Fig. 2, except that the invisible parts we recovered is colored with the rainbow colormap for better clarity.
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<thead>
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<th>Ours</th>
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</thead>
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<td><img src="image2" alt="frame L-1" /></td>
</tr>
<tr>
<td><img src="image3" alt="frame 0" /></td>
<td><img src="image4" alt="frame L-1" /></td>
</tr>
<tr>
<td><img src="image5" alt="frame 0" /></td>
<td><img src="image6" alt="frame L-1" /></td>
</tr>
</tbody>
</table>

Figure 2: **More results on natural sequences.** For each sample sequence, we show the first and last frame of the sequence (first row), the recovered shape and camera poses in two views (middle row) and the reprojected points onto the first and last frame, colored with the inverse depths (brighter is closer). For the recovered shape, we color the visible points with pixel values from the frames, and the invisible points with grey.

### 2.3. Failure Analysis

We show 4 failure cases of our methods in Fig. 4.

(1) Bad style initialization. We show in the first row that when
the object is of rare style and the style initialization gives wrong prediction, the entire shape would be carried away during optimization. (2) Bad pose initialization. In the second row we reproject the shape with estimated camera back to the first frame at initialization and convergence, and we show that although the pose is improved during optimization in face of wrong initialization, it is stuck at local minimum. (3) Large motion. Large motion introduce serious self-occlusion which breaks the photometric consistency assumption. The reprojection is done on the last frame and the recovered scene is also showed (third row). The camera poses are off for the last few frames when our method is not able to align these frames back to the template frame due to large motion. (4) Lighting change. This also breaks the photometric consistency assumption. We show in the fourth row the reprojection onto the last frame and the recovered scene.

2.4. Error Terms in the Objective

We show in Table 1 the quantitative results on rendered sequences under different combination of the error terms in the objective. In addition, we also demonstrate for one natural sequence under different combination of objective terms in Fig. 5. With photometric error alone, the final pose is not optimal due to lighting change and transparent parts which break the photometric consistency part. In this case the depth error and/or silhouette error will help regularize the pose space, and meanwhile help improve the object style.

3. Appendix III. Network and Training details

We denote each fully-connected layer $fc(d)$ by its output dimension $d$, and 2D convolution layer by $conv2D(k, c, s)$ representing kernel size of $k$, strides of $s$ across two spatial axes, and $c$ channels. A reshape layer is represented as $reshape(output \text{ size})$. A LSTM layer is represented as $lstm(h, n)$ with $h$ denoting the number of units in LSTM and $n$ de-
<table>
<thead>
<tr>
<th>Rendered Sequences</th>
<th>Depth Error</th>
<th>Density</th>
<th>Cam. Location Error</th>
<th>Cam. Orientation Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ours (full objective)</td>
<td>0.0627</td>
<td>0.9342</td>
<td>0.0102</td>
<td>1.2343°</td>
</tr>
<tr>
<td>Ours ($\mathcal{L}_{ph}$)</td>
<td>0.0709</td>
<td>0.8502</td>
<td>0.0156</td>
<td>1.9889°</td>
</tr>
<tr>
<td>Ours ($\mathcal{L}<em>{ph} + \lambda_1\mathcal{L}</em>{cd}$)</td>
<td>0.0648</td>
<td>0.9403</td>
<td>0.0130</td>
<td>1.3433°</td>
</tr>
<tr>
<td>Ours ($\mathcal{L}<em>{ph} + \lambda_2\mathcal{L}</em>{invd}$)</td>
<td>0.0677</td>
<td>0.9306</td>
<td>0.0144</td>
<td>1.7457°</td>
</tr>
</tbody>
</table>

Table 1: Quantitative comparison on rendered sequences under different combination of error terms.

Figure 4: Failure cases.

3.1. The Shape Prior

The shape prior is trained as the generator of aligned points clouds sampled from ShapeNet [1]. The aligned shape encoder takes as input an $24576 \times 3$ tensor, and uses an encoder of the identical architecture as [11] to output an embedded feature of 1,024 dimension indicating style of the input shape, except that we take out the transformation layers considering transformation invariability should not and need not be picked up by the encoder. The generator is motivated by [3] with the following two stream of layers: (1) $fc(2048), fc(4096), fc(8192), fc(8192 \times 3), reshape(8192 \times 3)$. (2) $reshape(4 \times 4 \times 4 \times 64), conv2D(3, 256, 1), conv2D(3, 128, 1), conv2D(5, 64, 2), conv2D(5, 64, 2), conv2D(5, 32, 2), conv2D(5, 3, 2), reshape(16384 \times 3)$. The outputs from two streams are then concatenated together to form an output point cloud of shape $24576 \times 3$.

Layers in the encoder are batch batch normalized except the first convolution and last layer. LeakyReLU [10, 5] is the rectifier for all layers except the output layer which uses tanh.

3.2. The Recurrent Style Regressor

The architecture of our recurrent regressor is shown in Fig. 6. As shown in Fig. 6, our proposed network inside the green bounding box basically contains three principle components: convolutional layers, LSTM and fully-connected layers. The convolutional layers we used are identical to the convolutional layers in AlexNet [8] and we use Siamese structure for different frames. At the top of those convolutional cell, LSTM cell [9] is followed to process the temporal feature sequences. At the end of the sequence, fully-connected cell is followed to generate the final style vector. Specifically, convolutional cell is constructed by the following layers in orders: $conv2D(3, 64, 2), conv2D(3, 96, 2), conv2D(3, 128, 2), conv2D(3, 192, 2), conv2D(3, 256, 2)$. LSTM cell is constructed by a single layer: $lstm(2048, 1024)$ and fully-connected cell is constructed by three fully-connected layers: $fc(2048), fc(1024), fc(1024)$ The single image based regressor for comparison is basically an AlexNet with the last softmax regression layer removed.

The code is implemented using tensorflow. We adopt Adam [7] to optimize our network For hyperparameter settings in training procedure, we exploit a learning rate of $3e - 5$ with no decay and a batch size of 16 for both recurrent network and single image based regressor. The final model is trained for 45000 iterations, which takes nearly half a day using a GTX Titan Xp.

3.3. Image to Style/Pose Regressors

For rendered sequences, to allow for fair comparison with Zhu et al. [14], we use trained style and pose regressors from Zhu et al. [14] based on single image, but reformulate the camera model to our perspective camera model. We fol-
full objective \quad \mathcal{L}_{\text{ph}} \quad \mathcal{L}_{\text{ph}} + \lambda_1 \mathcal{L}_{\text{cd}} \quad \mathcal{L}_{\text{ph}} + \lambda_2 \mathcal{L}_{\text{invd}}

<table>
<thead>
<tr>
<th>frame 0</th>
<th>frame L-1</th>
<th>frame 0</th>
<th>frame L-1</th>
<th>frame 0</th>
<th>frame L-1</th>
<th>frame 0</th>
<th>frame L-1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input</td>
<td>Ours</td>
<td>Input</td>
<td>Ours</td>
<td>Input</td>
<td>Ours</td>
<td>Input</td>
<td>Ours</td>
</tr>
</tbody>
</table>

Figure 5: Result of one rendered sequence under different combination of error terms.

Figure 6: The structure of our recurrent architecture which is adapted from AlexNet [8]. The network in green indicates our style regressor which is basically a recurrent convolutional neural network. The yellow trapezoid and the blue rectangle represent the first five convolutional layers and the last three fully connected layers in AlexNet [8] respectively. The cyan rounded rectangle represents a single LSTM [9] cell with peephole.

low [13] to build the two architectures for style and pose regressors. The network parameters are adjusted to accommodate an input image of size $128 \times 128$.

The two regressors have identical architecture of convolution layers: conv2D(3, 64, 2), conv2D(3, 96, 2), conv2D(3, 128, 2), conv2D(3, 192, 2), conv2D(3, 256, 2). For the style regressor, an $fc(1024)$ connects the last convolution layer to the style parameters. For the pose regressor, $fc(6)$ is used instead. All but the first convolution layers are batch normalized, and rectified with LeakyReLU.

4. Appendix IV. Evaluation on Initialization

To demonstrate the strength of our recurrent style regressor among single-image based shape regressor, we conduct experiments on our synthetic data for the comparison between the two network architecture. For single-image shape reconstruction, we construct an AlexNet [8] which takes in the first frame as input and outputs a style vector with a length of 256 while our recurrent style regressor takes in a 15 frames sequence as input and output a style vector with a length of 256. We choose 3D Chamfer distance which is given in Equ. 1 as a criterion for evaluating the performance of our generated point cloud. Let $X_{gt} = x^{(i)}_{gt}$ be ground truth point cloud and $X = x^{(i)} = G(s)$ be the point cloud generated from style vector. For comparison, we re-implement the single-image based style regressor in [14] and trained on our data render by blender [14] using perspective camera. The final Chamfer distance on test set is reported in Table 2. Our recurrent style regressor is slightly better than single-image based style regressor used in [14, 13].

$$\mathcal{L}_{\text{cd}}(X_{gt}, G(s)) = \frac{1}{N} \sum_{x_{gt} \in X_{gt}} \min_{x \in G(s)} ||x_{gt} - x||_2^2$$

$$+ \sum_{x \in G(s)} \min_{x_{gt} \in X_{gt}} ||x_{gt} - x||_2^2$$

(1)
Table 2: Quantitative results on 3D Chamfer distance between ground truth point cloud and generated point clouds for initialization.

<table>
<thead>
<tr>
<th>$\mathcal{L}<em>{cd}(X</em>{gt}, \hat{G}(s))$</th>
<th>Single image</th>
<th>Ours(initial)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>3.69</td>
<td>3.20</td>
</tr>
</tbody>
</table>

To give an illustrative result on our initialization method, we visualized some qualitative results of our initialization on natural sequences containing model cars and real automobiles in Figure 7. For each row, a combination of RGB image of first frame, silhouette of first frame, template retrieved from our pose initialization, the closest CAD model retrieved from our style initialization is shown. As we can see in Figure 7, although the style retrieved from regressor is not very precise and sometimes different CAD model for the same car under different views, our style regressor is able to yield style prediction that are close in 3D shape.

Figure 7: Some of the initialization results on natural sequences are shown in this figure. Results on real cars in the wild are shown on the left while results on toy model cars are shown on the right. Each row contains a combination of RGB image of first frame, silhouette of first frame, template retrieved from our style & pose initialization. Despite color, the retrieved model are close in shape and appearance.

References


